An Approach to Contact Force Vector Determination and Its Implementation to Provide Intelligent Tactile Interaction with Environment

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Abstract. The force vector information is essential while collision avoidance planning through tactile feedback in autonomous or teleoperation mode. In this paper, we concentrate on the approach to calculation of the applied force vector at any point of the robot arm and its technical realization. Based on the presented force vector calculation flow, we obtained the experimental results validating the ability of the proposed method to trace the contact point position and to estimate force vector robustly and accurately.

Keywords: Human-Robot interaction, sensitive robot arm.

1 Introduction

Recently, the new generation of robots called "service robots" has been advancing rapidly and it is considered that in near future they will be introduced in human daily life environment to assist with hospital care, surgery operations, high-risk maintenance tasks, construction works, and office affairs. Along with voice and image recognition, the robot tactile ability becomes salient link in the chain of multimodal interaction with humans. Moreover, the robot sensor system enabling detection of the mechanical contact with object in unstructured dynamic environment is needed, because the occlusion in video and proximity sensor system can happen.

Conventional approaches to controlling the physical interaction between a manipulator and environment are based on impedance control of a robot arm according to applied force vector measured at the manipulator wrist [1]. However, the rest parts of the robot body (forearm, elbow, upper arm, shoulder, and torso) are presenting the significant danger not only for human being, but also for the robot structure itself. The ability to sense the physical contact can be attained by covering the robot surface with tactile skin [2].

With tactile sensing technology continuously evolving, different types of tactile sensors such as piezoelectric-polymer-film-based [2], flexible-polyester-sheet-based, optical [3], etc. have been designed. Such sensors can only detect the contact area and coarsely measure the spatial distribution of pressures perpendicular to a sensory area. Therefore, they are unable to supply contact force orientation information. The most

appropriate application of such tactile sensors is recognition of contact area gravity center and contact image pattern.

To realize safe physical contact of entire robot arm structure with human and to guarantee the collision avoidance during teleoperation, our primary idea is concentrated on design of a whole-sensitive robot arm (by using artificial skin and distributed torque sensors in each joint). When contact with environment occurs, manipulator automatically generates compliant motion according to the measured external force vector. The newly developed anthropomorphic manipulator having 4-DOF arm and 8-DOF hand (Fig. 1(c)) is capable to safely interact with environment wherever contact occurs on the robot arm surface. An operator sitting in cockpit (Fig. 1(a)) controls remote robot arm through manipulation of master robot arm (Fig. 1(b)).



Fig. 1. Robot teleoperation system

The paper focuses on approach to determination of the applied force vector at each point of the robot arm. This information is essential to plan collision avoidance trajectory, structure the environment, and communicate with humans intelligently. The proposed method takes advantages of the tactile sensor, enabling to detect coordinates of the contact point, and the distributed joint torque sensors to measure exerted torques and force vector direction on the entire robot arm surface (including joints). This method originates from human tactile system. Very fine special resolution of the human skin allows performing tactile discrimination of surface texture by fingertips. However, it has moderate ability to estimate the exerted force, the job that muscles do. They generate torque at the skeletal joints balancing such external forces as gravity, mechanical constraints of joints, inertial forces, and contact forces. Each muscle produces a torque at a joint that is the product of its contractile force and its moment arm at that joint [4]. Hence, by estimation of the tension of the corresponding muscles, we can define the acting force as well as the force direction.

The remainder of the paper is structured as follows. The sensory system and approach to contact point detection are presented in Section 2. The equations supporting analytical basis for the contact force vector calculations and experimental results

are given in Section 3. In Section 4, we briefly conclude the paper and discuss the future work.

2 Sensory System of the Developed Robot Arm

The robot arm is covered with Kinotex tactile sensor measuring the pressure intensity through amount of backscattered light by photodetector [5]. The sensitivity, resolution, and dynamic range of this artificial skin are comparable to those of a human. The taxels displaced with 21.5 mm in X and 22 mm in Y direction make up 6x10 array.

In order to recognize the contact region, we employed the watershed algorithm, an image processing segmentation technique that splits an image into areas based on the topology of the image [6]. The adopted algorithm is processed as follows: departing from the local maximum, the new taxel is included into the contact area only if within the 3x3 array surrounding it there is an other taxel of greater or equal pressure intensity already included into the water stream.

The accurate estimation of the contact point can be obtained by computing the center of gravity of the contact pattern $c(x_c, y_c)$ of the neighborhood Ω by:

$$c(x_{c}, y_{c}) = \left(\frac{\sum_{x, y \in \Omega} x_{i} f_{i}(x_{i}, y_{i})}{\sum_{x, y \in \Omega} f_{i}(x_{i}, y_{i})}, \frac{\sum_{x, y \in \Omega} y_{i} f_{i}(x_{i}, y_{i})}{\sum_{x, y \in \Omega} f_{i}(x_{i}, y_{i})}\right),$$
(1)

where $f_i(x_i, y_i)$ is the pressure intensity level of the taxel *i* with coordinates (x_i, y_i) [7].

Calculation findings of image gravity center are listed in Table 1.

| 0 0 0 15 0 0 | | Y, mm | Press | ure inte f_{ij} | ensity | $\Sigma x_{i,j} f_{i,j}$ | $\Sigma y_{i,j} f_{i,j}$ | x_c | y_c |
|---------------|--------------------------------------|----------|-------|-------------------|--------|--------------------------|--------------------------|-------|-------|
| | Ye 🧑 | 157 | 0 | 114 | 190 | 482985 | 607541 | 94.4 | 118.8 |
| | | 135 | 26 | 1303 | 755 | | | | |
| | | 113 | 56 | 859 | 463 | | | | |
| | | 91 | 553 | 796 | 0 | | | | |
| Digital image | <i>x_c</i> Visual image | X, mm | 43 | 75 | 106 | - | | | |

Table 1. Calculation results of image gravity center

In order to facilitate the realization of torque measurement in each arm joint, we developed new optical torque sensors having high reliability, high accuracy (even in electrically noisy environment), easy mounting procedure, low price and compact sizes [8]. The novelty of our method is application of the ultra-small size photointerrupter (PI) RPI-121 as sensitive element to measure relative motion of sensor components. The spring components were manufactured from one piece of AISI 4135 steel using wire electrical discharge machining. The optical torque sensor is set between

the driving shaft of the harmonic transmission and driven shaft of the joint (Fig. 2(a)). When the load is applied to the robot joint, the magnitude of the output signal from the PI corresponds to the exerted load.



Fig. 2. Torque sensor of the elbow joint and calibration results

The spring members attached to the first, second, and third/forth joints were designed to measure torque of \pm 12.5 Nm, \pm 10.5 Nm, \pm 4.5 Nm, and have resolution of 10.77 mNm, 9.02 mNm, 4.31 mNm, respectively. Each sensor was calibrated by means of attachment of reference weights to the lever arm. Calibration results for the elbow joins detector are given in Fig. 2 (b). Non-linearity of 2.5 % of Full Scale was calculated using maximum deviated value from the best-fit line.

3 Contact Force Vector Calculation Algorithm

In this section, we consider the problem of computing the force vector at any contact point on entire teleoperated robot arm based on the contact point coordinates and



Fig. 3. Coordinate system

output signal from the torque sensors. The coordinate systems fixed to the joints and connected to the arbitrary contact points are shown in Fig. 3. The forces ${}^{i}f_{i}$ acting in the coordinate system of each joint produce moments ${}^{i}n_{i}$ (Eq. 2). The joint torques are derived by taking Z component of the moments applied to the link (Eq. (4)).

$${}^{i}n_{i} = {}^{i}_{i+1}R^{i+1}n_{i+1} + {}^{i}P_{C_{i}} \times {}^{i}F_{i} + {}^{i}P_{i+1} \times {}^{i}_{i+1}R^{i+1}f_{i+1}$$
(2)

$${}^{i}f_{i} = {}^{i}_{i+1}R^{i+1}f_{i+1} + {}^{i}F_{i}$$
(3)

$$\tau_i = {}^i n_i^T \, {}^i \hat{Z}_i \ , \tag{4}$$

where $_{i+1}{}^{i}R$ is the matrix of rotation between links i+1 and i calculated using Denavit-Hartenberg notation; ${}^{i}P_{i+1}$, ${}^{i}P_{Ci}$ are the vectors locating the origin of the coordinate system i+1 in the system i, and contact point, respectively; ${}^{i}F_{i}$ is the contact force.

Let us consider the case when external force is applied to the upper arm of the robot. Using the Eq. (2), (3) we have:

$${}^{2}n_{2} = \begin{bmatrix} 0\\L_{F2}\\0 \end{bmatrix} \times \begin{bmatrix} F_{2x}\\F_{2y}\\F_{2z} \end{bmatrix} = \begin{bmatrix} L_{F2}F_{2z}\\0\\-L_{F2}F_{2x} \end{bmatrix}; \quad {}^{1}n_{1} = \begin{bmatrix} s_{2} & c_{2} & 0\\0 & 0 & 1\\c_{2} & -s_{2} & 0 \end{bmatrix} \begin{bmatrix} L_{F2}F_{2z}\\0\\-L_{F2}F_{2x} \end{bmatrix} = \begin{bmatrix} L_{F2}F_{2z}s_{2}\\-L_{F2}F_{2x}\\L_{F2}F_{2z}c_{2} \end{bmatrix}.$$
(5)

The components of the applied force vector and force magnitude are derived from:

$$F_{2x} = \tau_2 / (-L_{F2}) ; F_{2z} = \tau_1 / (L_{F2}c_2) ; F_2 = \sqrt{(F_{2x})^2 + (F_{2z})^2} .$$
 (6)

The value of the applied force projection on the axis Y is not required because the upper arm cannot move in this direction. For the case when the force acts on the forearm we have the following algorithm to obtain the contact force vector:

$$F_{4x} = \tau_4 / L_{F4} ; F_{4z} = \tau_3 / (L_{F4} s_4);$$

$$F_{4y} = (\tau_2 + F_{4z} (L_{F4} c_3 c_4 + L_2 c_3) + F_{4x} (L_{F4} s_3 + L_2 s_3 c_4)) / (L_2 s_3 s_4),$$
(7)

where c_2 , c_3 , c_4 , s_3 , and s_4 are abbreviations for $cos(\theta_2)$, $cos(\theta_3)$, $cos(\theta_4)$, $sin(\theta_3)$, and $sin(\theta_4)$, respectively; L_2 , L_{F2} , and L_{F4} are the lengths of the moment arms.



Fig. 4. Torque sensor of the elbow joint and elbow joint assembly

To evaluate the feasibility of the proposed approach, the experiments were conducted for calculation of the contact force vector acting on the upper arm.

During the experiment the object was moved along the upper arm surface according to the curve shown in Fig. 4(c). While contacting, the torques values measured at the first and second joint (τ_1 , τ_2) varies in accordance with Fig. 4(a). The contact force vector projections (F_{2x} , F_{2z}) and force vector length F_2 obtained from Eq. (6) are represented in Fig. 4(b). The trajectory of the end point of the contact force vector is shown in Fig. 4(c).

4 Discussion of Experimental Results and Future Work

The experimental results show that the developed algorithm and implemented sensory system of the robot arm allow measuring the force direction at any point of the robot arm accurately and robustly. For further enhancement of the contact point position estimation, the tactile sensor with higher spatial resolution is required.

In the future research we are going to employ the information on force vector and contact point to plan the compliant collision avoidance trajectory autonomously and provide tactile feedback to the operator through electro-stimulating device. We consider that presenting the information about direction and intensity of the contact force vector can greatly improve the collision avoidance strategy realized by operator, in comparison with the conventional contact area tactile feedback. On the next stage we will also develop such kind of control that allows rounding the contacting surface by using force vector value and pressure distribution at the contact area.

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